

2.56. Model: The cars are represented as particles.

Visualize:

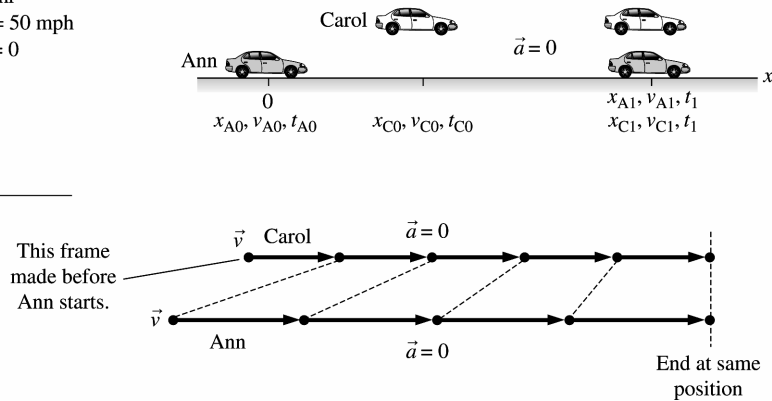
Known

$$\begin{aligned} x_{A0} &= 0 & t_{A0} &= 0.5 \text{ hr} \\ a_A &= 0 & v_{A0} &= v_{A1} = 50 \text{ mph} \\ x_{C0} &= 2.4 \text{ mi} & t_{C0} &= 0 \\ a_C &= 0 \\ v_{C0} &= v_{C1} = 36 \text{ mph} \end{aligned}$$

Find

$$\begin{aligned} t_1 &\text{ when } x_{A1} = x_{C1} \\ x_1 &= x_{A1} = x_{C1} \end{aligned}$$

Pictorial representation



Solve: (a) Ann and Carol start from different locations at different times and drive at different speeds. But at time t_1 they have the *same* position. It is important in a problem such as this to express information in terms of *positions* (that is, coordinates) rather than distances. Each drives at a constant velocity, so using constant velocity kinematics gives

$$x_{A1} = x_{A0} + v_A(t_1 - t_{A0}) = v_A(t_1 - t_{A0}) \quad x_{C1} = x_{C0} + v_C(t_1 - t_{C0}) = x_{C0} + v_C t_1$$

The critical piece of information is that Ann and Carol have the same position at t_1 , so $x_{A1} = x_{C1}$. Equating these two expressions, we can solve for the time t_1 when Ann passes Carol:

$$\begin{aligned} v_A(t_1 - t_{A0}) &= x_{C0} + v_C t_1 \\ \Rightarrow (v_A - v_C)t_1 &= x_{C0} + v_A t_{A0} \\ \Rightarrow t_1 &= \frac{x_{C0} + v_A t_{A0}}{v_A - v_C} = \frac{2.4 \text{ mi} + (50 \text{ mph})(0.5 \text{ h})}{50 \text{ mph} - 36 \text{ mph}} = 2.0 \text{ h} \end{aligned}$$

(b) Their position is $x_1 = x_{A1} = x_{C1} = x_{C0} + v_C t_1 = 74$ miles.

(c) Note that Ann's graph doesn't start until $t = 0.5$ hours, but her graph has a steeper slope so it intersects Carol's graph at $t \approx 2.0$ hours.